

FULL INSURANCE / RISK SHARING

↓

Each region should get $y + \frac{1}{2}$ every time

$$y_1 + \frac{1}{2} + y_2 + \frac{1}{2}$$

Requires region with $y+1$ to give away $\frac{1}{2}$ to the other region.

But will the region do so?

If you're stuck, I have 2 options:

- Stay with risk sharing agreement $v(y + \frac{1}{2}) + \delta v^s$

- If I leave (defect): $v(y+1) + \delta v^d$

v_1 v_2 v_3 How we trade off utilities in time?

$$V = v_0 + \delta v_1 + \delta^2 v_2 + \delta^3 v_3 \dots$$

Total
lifetime
utility

$\delta < 1$ discount factor

$$= v_0 + \delta [v_1 + \delta v_2 + \delta^2 v_3 \dots]$$

$v_1 \rightarrow$ utility tomorrow

There are different consequences if we STAY or DEFECT

- STAY

$$v(y + \frac{1}{2}) + \delta v(y + \frac{1}{2}) + \dots +$$

So

$$v(y + \frac{1}{2}) [1 + \delta + \delta^2 + \delta^3 + \dots] \rightarrow \text{the utility will be the same in each period}$$
$$= \frac{1}{1 - \delta}$$

$$v(y + \frac{1}{2}) + \frac{d}{1-d} v(y + \frac{1}{2})$$

EXCLUDED FOR T PERIODS (DEFECTED)

$$V_0^d = E[V_0] + d E[V_1] + \dots + d^t E[V_t] + d^{t+1} v(y + \frac{1}{2})$$

$$= E[V] \{ 1 + d + d^2 + \dots + d^t \} \rightarrow \frac{1 - d^{t+1}}{1-d}$$

$$v(y + \frac{1}{2}) \{ d^{t+1} + d^{t+2} + \dots \} \rightarrow v(y + \frac{1}{2}) d^{t+1} [1 + d + d^2 + \dots]$$

So I can have $1 + d + d^2 + \dots + d^t + d^{t+1} + d^{t+2} + \dots \rightarrow \frac{d^{t+1}}{1-d}$

OR $- d^{t+1} - d^{t+2} - \dots$

$$= - d^{t+1} \underbrace{[1 + d + d^2 + \dots]}_{\frac{1}{1-d}} = \frac{1}{1-d} - \frac{d^{t+1}}{1-d} = \frac{1 - d^{t+1}}{1-d}$$

↑
exclusion period

SO WHEN I AM EXCLUDED:

$$v(y + \frac{1}{2}) + d \left[\frac{1 - d^{t+1}}{1-d} E[v(y)] + \frac{d^{t+1}}{1-d} v(y + \frac{1}{2}) \right]$$

3 Would stay ^{in the risk sharing} if:

$$v(y + \frac{1}{2}) + \frac{d}{1-d} v(y + \frac{1}{2}) \geq v(y + \frac{1}{2}) + \frac{d}{1-d} \left[(1 - d^{t+1}) E[v(y)] + d^{t+1} v(y + \frac{1}{2}) \right]$$

$$v(y + \frac{1}{2}) \geq (1-d) v(y + \frac{1}{2}) + d \left[(1 - d^{t+1}) E[v(y)] + d^{t+1} v(y + \frac{1}{2}) \right]$$

SMALLER $\delta \Rightarrow$ right-hand side larger
 \Rightarrow more likely to defect

LARGER $T \Rightarrow$ Right-hand side smaller \Rightarrow less likely to defect

more risk
adverse

$v(y + \frac{1}{2}) \gg E[V] \Rightarrow$ right-hand smaller
 \uparrow
larger

22/03/2017

TAXATION : TAX COMPETITION

CAPITALIST MOBILE

A SMALL OPEN ECONOMY

FIX AMOUNT OF CAPITAL AVAILABLE that can be invested in production or local market

it's a quantity $\bar{K} = K + K^g$
 \swarrow home investment \searrow investment in global market
 \rightarrow demand is fixed, so if I invest more in K , I invest less in K^g

The decision is if to invest in home or abroad (in market)

- PRODUCTION (function of capital and labour)

$F(K, L)$

$$F = K^\alpha \cdot L^{1-\alpha}$$

L can be the hours of work, people employed

Investment decision

I have to maximize my profit by choosing how much to invest in K and K^g

LABOUR IS FIXED

If I invest in home; if I invest in global market

$$F(k, L) - wL + \rho k^d - t k$$

wage rate

world market rate

the investor has to pay taxes on capital

$$F(k, L) - wL + \rho(\bar{k} - k) - t k$$

→ marginal product of capital

~~the only variable is K, L~~

The company can choose L (that in equilibrium is constant)

$$\frac{\partial}{\partial k} = \frac{\partial F(k, L)}{\partial k} - \rho - t = 0$$

$$\frac{\partial}{\partial L} = \frac{\partial F(k, L)}{\partial L} - w = 0$$

$$\frac{F}{L} = k^{+\alpha} L^{-\alpha} = \left(\frac{k}{L}\right)^{\alpha}$$

$$\frac{F(k, L)}{L} = F\left(\frac{k}{L}, 1\right)$$

Homogeneous of degree 1

Constant returns to scale

Homogeneous function: $F(\lambda k, \lambda L) = \lambda^s F(k, L)$ Homogeneous of degree s

IF $s = 1 \rightarrow$ constant return to scale

$$\frac{\partial}{\partial \lambda} = \frac{\partial F(\lambda k, \lambda L)}{\partial(\lambda k)} \cdot k + \frac{\partial F(\lambda k, \lambda L)}{\partial(\lambda L)} \cdot L = F(k, L)$$

Must hold for all λ including $\lambda = 1$

$$\frac{\partial F}{\partial k} \cdot k + \frac{\partial F}{\partial L} \cdot L = F$$

Differentiate wrt k

$$\frac{\partial}{\partial k} = \frac{\partial F}{\partial (\lambda k)} \cdot \lambda = \lambda \cdot \frac{\partial F}{\partial k}$$

$$\frac{\partial F(\lambda k, \lambda L)}{\partial (\lambda k)} = \frac{\partial F(k, L)}{\partial k} \quad \text{set } \lambda = \frac{1}{L}$$

$$\frac{\partial F\left(\frac{k}{L}, 1\right)}{\partial \left(\frac{k}{L}\right)} = \frac{\partial F(k, L)}{\partial k}$$

↓

capital's marginal product is a function of $\frac{k}{L} \equiv k$

$$F(k) = \frac{F(k, L)}{L} = F\left(\frac{k}{L}, 1\right)$$

↓
per capital capital

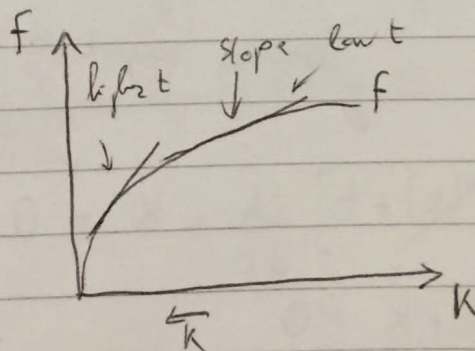
per capital production is a function of per capital capital

$$\Rightarrow F'(k) - p - t = 0$$

per capital production

↓
k is an implicit function of t

If I have a concave production technology; it will look:



if $t \uparrow$, $k \downarrow$

If taxes increase, less capitalist will be attracted

$$\Rightarrow F''(k) dk - dt = 0$$

$$\Rightarrow \frac{dk}{dt} = \frac{1}{F''(k)} < 0$$

negative second derivate for concave function

So reducing taxes will encourage investments

NOW SEE WHAT GOVERNMENT WILL DO ON t

$$\text{MAX}_t \frac{wL}{L} + \frac{tK}{L}$$

is the same if I maximize for capital

$$\text{MAX}_t w + tK$$

$$w = \frac{\partial F}{\partial L}$$

$$wL = F - \frac{\partial F}{\partial K} \cdot K$$

total production

what capital owners earn

$$w = \frac{F}{L} - \frac{\partial F}{\partial K} \cdot \frac{K}{L} = F(k) - F'(k) \cdot k$$

$$\text{max}_t F(k) - F'(k) \cdot k + tK$$

government maximizes \hat{w} plus tax

k is function of t

derivate respect to t

ideally

$$\Rightarrow \left[\cancel{F'(k)} - \cancel{F''(k) \cdot k} - \cancel{F'(k)} + t \right] \frac{dk}{dt} + k = 0$$

$$(-F''(k) \cdot k + t) \frac{dk}{dt} + k = 0$$

$$-\frac{F''(k) \cdot k + t}{F''(k)} + k = 0$$

$$-\cancel{k} + \frac{t}{F''(k)} + \cancel{k} = 0$$

$$\Rightarrow \frac{t}{F''(k)} = 0$$

↓
denominator is negative

$$t = 0$$

↓

the best thing I can do is not tax at all

~~I can push my tax negative~~

TWO ECONOMIES (NO COOPERATION)

$$\bar{k} = k^1 + k^2$$

$$\cancel{F(k, L) - w}$$

$$\cancel{F(k) - w}$$

3 can invest in region one or two

$$F(k^1, L^1) - w^1 L^1 - t^1 k^1 + F(k^2, L^2) - w^2 L^2 - \underset{\substack{\downarrow \\ k - k^1}}{t^2 k^2}$$

$$\frac{\partial}{\partial k^1} = \frac{\partial F(k^1, L^1)}{\partial k^1} - t^1 + \frac{\partial F(k^2, L^2)}{\partial k^2} (-1) + t^2 = 0$$

$$\Rightarrow F'(k^1) - t^1 - F'(k^2) + t^2 = 0$$

$$F'(k^1) - t^1 - F'(\bar{k} - k^1) + t^2 = 0 \quad *$$

REGION ONE FIRST

$$\max_{t^1} F(k^1) - F'(k^1)k^1 + t^1 k^1$$

take t^2 as given

→ the consequences are given also by region TWO; and the same for region ONE (independence)

Whatever the other government decides, I have to do what is optimal for me.

NASH EQUILIBRIUM

$$[-F''(k^1)k^1 - F'(k^1) + t^1] \frac{dk^1}{dt^1} + k^1 = 0 \quad \text{THIS BEFORE}$$

NOW

$$* [F''(k^1) + F''(\bar{k} - k^1)] dk^1 - dt^1 = 0$$

$$\frac{dk^1}{dt^1} = \frac{1}{F''(k^1) + F''(k^2)}$$

$$\frac{-F''(k^1)k^1 + t^1}{F''(k^1) + F''(k^2)} + k^1 = 0$$

~~$$\frac{-F''(k^1)k^1 + t^1 + k^1 F''(k^1) + k^1 F''(k^2)}{F''(k^1) + F''(k^2)} = 0$$~~

$$t^1 + k^1 F''(k^2) = 0$$

$$\Rightarrow t^1 = -k^1 F''(k^2) > 0$$

$$\Rightarrow t^2 = -k^2 F''(k^1) > 0$$

Contrary to open economy, here it is possible to impose taxes

CENTRAL GOVERNMENT

$$t^1 = -\frac{\bar{k}}{2} F''\left(\frac{\bar{k}}{2}\right) > 0$$

$$t^2 = -\frac{\bar{k}}{2} F''\left(\frac{\bar{k}}{2}\right) > 0$$

$$Z \left(F\left(\frac{\bar{k}}{2}\right) - F'\left(\frac{\bar{k}}{2}\right) \frac{\bar{k}}{2} + t \frac{\bar{k}}{2} \right)$$

$$\frac{\partial}{\partial t} = \frac{\bar{k}}{2} > 0 \quad \text{it's more than two separate governments}$$

PESTIEAU

ECONOMICS OF SOCIAL PROTECTION

INTRODUCTION

A Design and sustainability

THREE SOCIAL POLICIES

B Performance of social protection

C social protection and private insurance

D Zapping, transfer kind and workforce

OBJECTIVES

• PROTECTION AGAINST LIFETIME RISKS

- DISABILITY

- FAMILY

- EARLY / LATE DEATH

• POVERTY AND INEQUALITY ALLEVIATION

RELATIVE VS ABSOLUTE

TEMPORARY VS